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**Deformation theory of sandwiched singularities.**

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This paper deals with the study of deformations of sandwiched singularities, a class of surface singularities introduced by Hironaka. The authors develop a geometric method, called the “picture method”, for studying such deformations. By means of this method they can, without a great deal of calculation, construct many “different” smoothings of sandwiched singularities and study many of their properties. To give just one example, they have a geometric construction of the Milnor fibre, enabling them to compute the homology and the intersection form of the Milnor fibre.

Reviewed by *Gerhard Pfister*

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